

# Statistical Reasoning

Week 4

Sciences Po - Louis de Charsonville

Spring 2018

Research Paper

Distributions and graphs

Measures of central tendency

Mean

Median

Mode

Measures of Variability

Range(s)

Standard deviation

Normal distribution

# Research Paper

## Timeline

Research Proposal	<b>Today</b>
1 <sup>st</sup> draft	<b>6 March</b>
2 <sup>nd</sup> draft	<b>10 April</b>
<b>Final draft</b>	<b>24 April</b>

## Submission's Rules

- ▶ A **word** document (following template on the Google Drive).
- ▶ A **do-file** showing *all* commands in Stata with comments in green.

# The Word document

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- ▶ Provisional paper title
- ▶ Introduction stating and accounting the research question
- ▶ Brief theory section describing your hypotheses
  - ▶ Describe how you think the independent variable you chose are supposed to influence the dependent variable (better if you have a few references).
- ▶ Brief description of the dataset
  - ▶ Objectives of the survey, date, data collecting methods, sampling, etc.
- ▶ Description of the dependent and independent variables as they exist unmodified in the original data
  - ▶ Names, codes, values, what they measure, missing values
- ▶ Description of all variable renamings, recodings, how missing values have been managed ;
- ▶ Univariate statistics on all variables with 1/2 sentence(s) describing their distribution.

# Exporting results from Stata into Word

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- ▶ Tables : select copy table, paste in Excel, edit, paste in Word.
  - ▶ Add footnotes.
- ▶ Graphs : save in .tif format, insert as a picture in Word
- ▶ *More details* : section 13.4 in the **Stata Guide**.

# Distributions and graphs

# Distributions

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- ▶ A distribution is a collection of data, or scores, on a variable.
- ▶ Scores are usually arranged in order from smallest to largest.

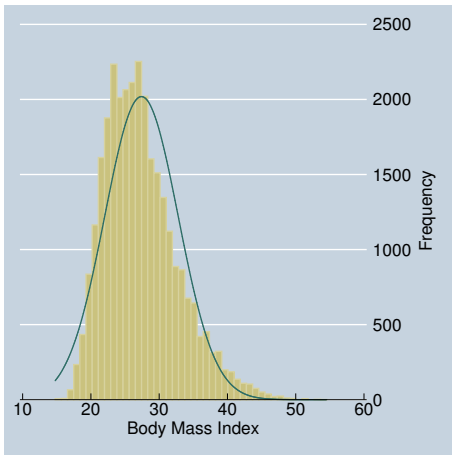


Figure – Distribution of BMI



## Example - Gun control in the US

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Would you like to see gun laws in the US made more strict, less strict, or remain as they are?

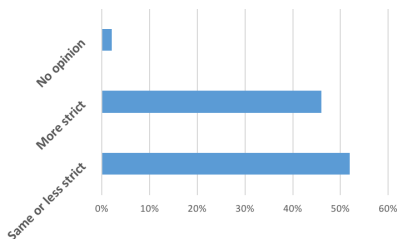
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- ▶ more strict : 46%
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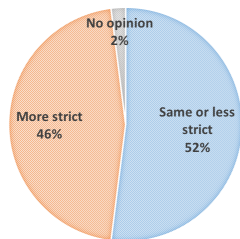
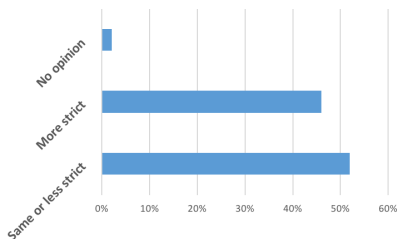


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## Frequency distributions

- ▶ Provide the number of observations in each category and/or the corresponding percentage
  - ▶ Be careful : percentages should sum to 100%
  - ▶ How have you dealt with *missing values* ?
- ▶ **Cumulative frequencies or percentages** : provide the number/percentage of observations below or equal to a given value or category (only with *ordinal data*)
- ▶ **Stata** : these statistics are obtained with `tab` or `fre`, and can be visualized using **bar graphs** and **histograms**

# Distribution of Quantitative Variables

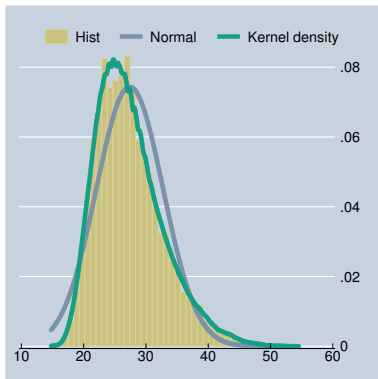
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  - ▶ Example : earnings in `nhis9711`
- ▶ Compute measures of central tendency and variability.
- ▶ Plot the probability density function (*kernel density*)

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# Measures of central tendency

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- ▶ Collection of scores of a variable : **distribution**
- ▶ How spread out the scores are ?
- ▶ What is the most common score ?
- ▶ etc.

One set of distribution characteristics that research are interested in is **central tendency** :

- ▶ mean
- ▶ median
- ▶ mode

## Stata

- ▶ use `sum` or `tabstat`
- ▶ *primarily appropriate for quantitative variables*



# Mean

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- ▶ Arithmetic average of a distribution of scores :

$$\bar{x} = \sum_{i=1}^N \omega_i x_i, \text{ with } \omega_i \text{ weight of obs } i$$

- ▶ Most commonly used
- ▶ Denoted  $\mu$  for the *population mean* and  $\bar{x}$  for the *sample mean*

## Weaknesses

- ▶ Sensitive to extreme values (*outliers*)
- ▶ A distribution may have very few scores near the mean

# Mean

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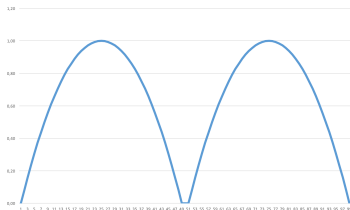
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$$X_1 = \{2, 3, 5, 6\}$$

$$X_2 = \{0, 3, 5, 8\}$$

$X_1, X_2$  have the same mean.

# Median

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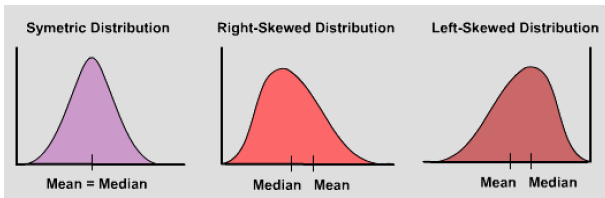
- ▶ The score in the distribution that marks the 50th percentile
- ▶ 50% of the scores in the distribution fall above the median and 50% fall below it.
- ▶ Not sensitive to outliers.
- ▶ Comparing the mean and the median gives an idea whether the distribution is skewed or not.

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## Skewed or not ?



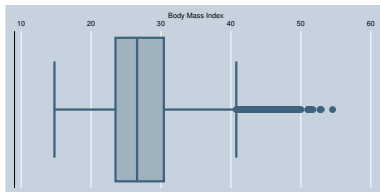
# Beyond the median

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- ▶ **Quartiles** : divide the sample into 4 equal parts
- ▶ **Deciles** : divide the sample into 10 equal parts
- ▶ **Percentiles** : divide the sample into 100 equal parts.

## Stata

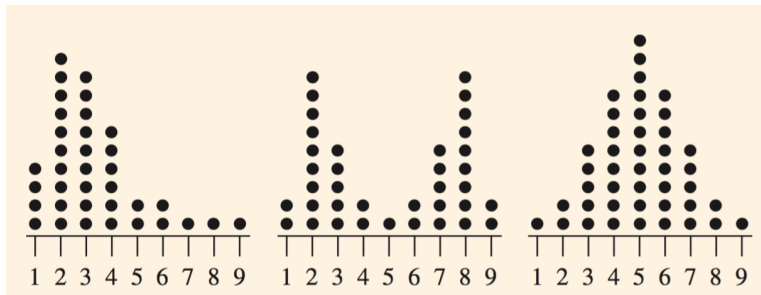
- ▶ use `summarize` (with options `details`)
- ▶ or draw a boxplot with `graph hbox`



# Mode

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- ▶ The **most frequent value** in the sample
- ▶ A series of values can be unimodal (one mode), bimodal (two modes) or multimodal (several modes).
- ▶ Not used a lot.



# Example

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$$X = \{86, 90, 95, 100, 100, 110, 110, 115, 120\}$$

- ▶ Mean ?
- ▶ Median ?
- ▶ Unimodal ? Bimodal ?

## Stata

- ▶ Use the **mean** for continuous variables `su`
- ▶ Use the **median** when there are outliers `su, d`
- ▶ Use the **mode** for categorical variables `fre`



# Measures of Variability

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## Old saying

*"If your head is in the freezer and your feet are in the oven, on average you're comfortable."*

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- ▶ Measures of central tendency do not inform us on the dispersion of scores in the distribution

## Measures of dispersions

- ▶ Range
- ▶ Variance
- ▶ Standard deviation (most informative and widely used)

# Range

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- ▶ Range = difference between the largest score and the smallest score.

$$\textit{Range} = \textit{Max} - \textit{Min}$$

# Range

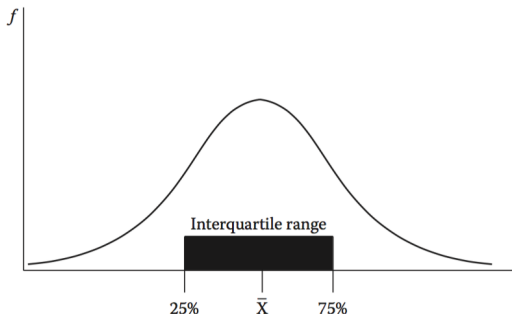
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- ▶ Range = difference between the largest score and the smallest score.

$$\text{Range} = \text{Max} - \text{Min}$$

- ▶ Another common measure : **Interquartile range (IQR)** :

$$\text{IQR} = Q_3 - Q_1$$



# Standard deviation

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- ▶ **Deviation** : refers to the distance between an individual score and in the average score
- ▶ **Standard** : means *average*
- ▶ Standard deviation is the average distance between individual observation and the mean of the distribution.

## Formula

*Population* :

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}}$$

Estimate based on a *sample* :

$$\sigma = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}}$$

The shape of the distribution refers to how the observations are distributed around the mean

- ▶ symmetrically distributed ?
- ▶ Are they widely spread around the mean ? (Outliers ?)

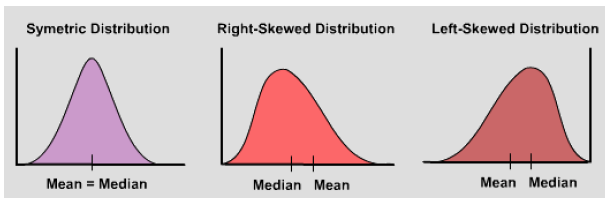
**Describing the shape :**

- ▶ Skewness (asymmetry)
- ▶ Kurtosis (flatness)

# Skewness

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- ▶ **Right-skewed** (*positive skew*) : outliers pull the mean upwards (a few very high values), graphically the mean is pulled to the right, the right-hand tail is longer. Most observations are clustered at the lower end.
- ▶ **Left-skewed** (*negative skew*) : outliers pull the mean downwards (a few very low values), graphically the mean is pulled to the left, the left-hand tail is longer. Most observations are clustered at the higher end.



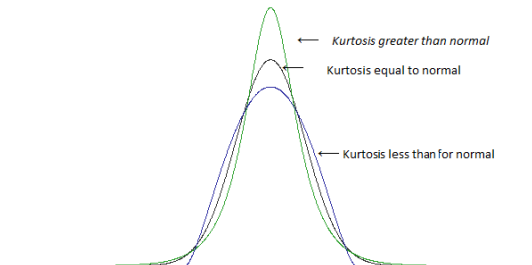


# Kurtosis

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The shape of a distribution of scores in terms of its flatness or peakedness (compared to the normal distribution)

- ▶ A normal distribution has a kurtosis of 3.
- ▶ **Leptokurtic** : a higher peak and thinner tails (than the normal curve, *kurtosis* > 3)
- ▶ **Platykurtic** : a lower peak and thicker tails (than the normal curve, *kurtosis* < 3)



# Normal distribution

# Normal distribution $\mathcal{N}(\mu, \sigma^2)$

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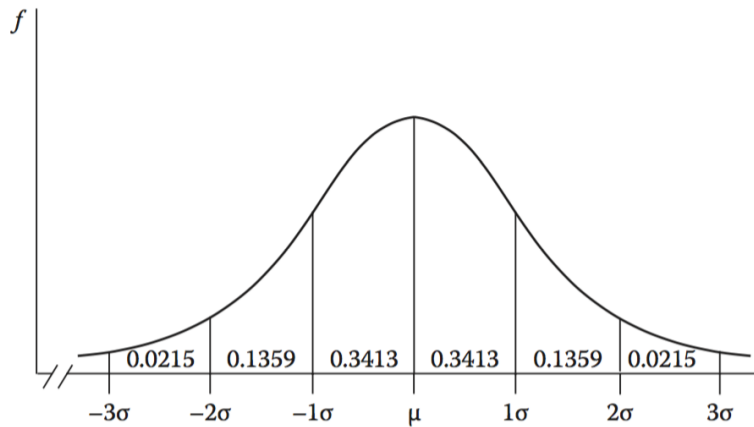
- ▶ **Normal distribution** : extremely important to statistics
- ▶ often referred as the **bell curve**

## Properties

- ▶ **symmetric** and **unimodal**
- ▶ **mean = median = mode**
- ▶  $\mathcal{N}(0, 1)$  **standard normal distribution**

# Normal curve

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# Normality assessment

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## Visual assessment

- ▶ Distributions `hist, normal, kdensity, gr (h)box`
- ▶ Diagnostics `symplot, qnorm, g(ladder)`

## Formal assessment

- ▶ Use `su x, d` to assess the symmetry (*skewness*  $\sim 0$ ) and flatness (*kurtosis*  $\sim 3$ ) of a variable.
- ▶ Use `tabstat x y, s(skew kurt) c(s)` to compare a variable with its transformation (often to log-units)

# PRACTICE